

## Bell Ringer

Identify the asymptotes for each of the following equations.

$$f(x) = \frac{2x' + 3}{x' - 4}$$

$$\begin{aligned}x - 4 &= 0 \\x &= 4\end{aligned}$$

$$VA \Rightarrow x = 4$$

$$HA: y = \frac{2}{1} = 2$$

$$\begin{array}{r}3x + 1 \\x - 1 \overline{) 3x^2 - 2x + 4} \\ \underline{-3x^2 - 3x} \phantom{+ 4} \\ \phantom{-3x^2} + 7x + 4 \\ \phantom{-3x^2} \underline{-7x - 7} \\ \phantom{-3x^2} \phantom{+ 7x} + 11\end{array}$$

$$g(x) = \frac{3x^2 - 2x + 4}{x - 1}$$

$$VA: x = 1$$

$$HA: \text{NO}$$

$$SA: y = 3x + 1$$

# Lesson 3.8

Objectives:

## Types of Variation

- Direct Variation: If y varies directly from x, then we will use the equation,

$$\frac{y_1}{x_1} = \frac{y_2}{x_2}$$

- Inverse Variation: If y varies inversely from x, then we will use the equation,

$$\frac{y_1}{x_2} = \frac{y_2}{x_1}$$

- Joint Variation: If y varies jointly from x and z, then we will use the equation,

$$\frac{y_1}{y_2} = \frac{x_1 z_1}{x_2 z_2}$$

Suppose  $y$  varies directly as  $x$  and  $y = 14$  when  $x = 8$ .

Use the equation to find the value of  $y$  when  $x = 4$ .

$$\frac{y_1}{x_1} = \frac{y_2}{x_2} \rightarrow \frac{14}{8} = \frac{y}{4}$$

$$56 = 8y$$
$$\textcircled{7} = y$$

**If  $y$  varies inversely as  $x$  and  $y = 102$  when  $x = 7$ ,  
find  $x$  when  $y = 12$ .**

$$\frac{102}{x} = \frac{12}{7}$$

$$12x = 714$$

$$x = 59.5$$

If  $y$  varies jointly as  $x$  and the cube of  $z$  and  $y = 16$  when  $x = 4$  and  $z = 2$ , find  $y$  when  $x = -8$  and  $z = -3$ .

$$\frac{y_1}{y_2} = \frac{x_1(z_1)^3}{x_2(z_2)^3} \Rightarrow \frac{16}{y} = \frac{4 \cdot (2)^3}{-8 \cdot (-3)^3}$$

<sup>32</sup>  
216

$$\frac{32y}{32} = \frac{3456}{32}$$

$$y = 108$$

If  $r$  varies inversely as  $t$  and  $r = 3$  when  $t = 4$ , find  $r$  when  $t = 15$ .

$$\frac{r_1}{t_2} = \frac{r_2}{t_1}$$

$$\frac{3}{15} = \frac{r}{4} \Rightarrow 12 = 15r$$
$$\frac{4}{5} = \frac{12}{15} = r$$

If  $y$  varies directly as the square of  $x$  and  $y = -54$  when  $x = 9$ , find  $y$  when  $x = 6$ .

$$\frac{y_1}{(x_1)^2} = \frac{y_2}{(x_2)^2}$$

$$\frac{-54}{9^2} = \frac{y}{6^2}$$

$$81y = -1944$$

$$y = -24$$



3.8 # 5-10

Page 194 # 13-19